

# END TERM EXAMINATION

FIRST SEMESTER [BCA] DECEMBER 2024

Paper Code: BCA-101

Subject: Discrete Mathematics

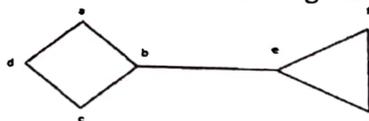
Time: 3 Hours

Maximum Marks: 60

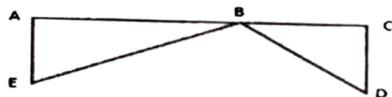
Note: Attempt all questions as directed.

Q1 Answer Any Five from the following:

- a) Verify De-Morgan's Law for universal set  $U=\{1,2,3,4,5,6,7\}$ ,  $A=\{4,1,2,5\}$  and  $B=\{1,2,4,6\}$ . (4)
- b) Define Hamiltonian circuit and Hamiltonian Path with example. (4)
- c) Draw the Hasse diagram representing the partial ordering  $(P(A):\subseteq)$ , where  $A=\{1,2\}$  (4)
- d) Let  $A=\{1,2,5,6\}$ ,  $B=\{2,5,7\}$ ,  $C=\{1,3,5,7,9\}$ . Verify  $(A \times B) \cap (A \times C) = A \times (B \cap C)$  (4)
- e) Represent G, considering the graph  $G(V, E)$  where V consist of 4 vertices A, B, C and D of five edges Where  $e_1 = \{A, B\}$ ,  $e_2 = \{B, C\}$ ,  $e_3 = \{C, D\}$ ,  $e_4 = \{A, C\}$ ,  $e_5 = \{B, D\}$  (4)
- f) Find radius and diameter of the given diagram (4)



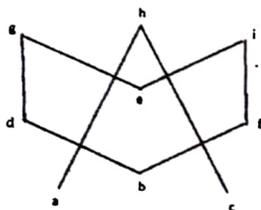
- g) Draw the complete graph of  $W_5$  and  $K_5$ . Also define Euler's circuit and determine whether the graphs shown is a Euler's circuit or not. (Give reason) (4)



- h) Find the explicit formula for the sequence 67, 65, 63, 61, 59. (4)

- Q2 a) Suppose that  $A= \{1, 2, 3\}$  and  $B= \{1, 2\}$ . Let R be a relation from A to B containing  $(a,b)$  if  $a \in A$ ,  $b \in B$  and  $a > b$ . Do Matrix representation of  $M_R^{-1}$  (5)
- $M_R$  and  $M_{R^c}$  of the relation R.
- b) Construct the truth table (5)
- i)  $(\neg q \rightarrow \neg p) \rightarrow (p \rightarrow q)$
  - ii)  $(\neg p \vee q) \vee \neg p$
- Is given proposition is Tautology. (5)

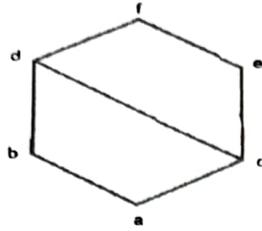
- Q3 a) Find lower bound, upper bound, least upper bound, greatest lower bound of the sets  $\{d,e,f\}$ ,  $\{a,c\}$  and  $\{b,d\}$  of given graph. (5)



P-1/2

P.T.O.

b) Give reason why given lattice is a distributed lattice but not a complemented lattice.



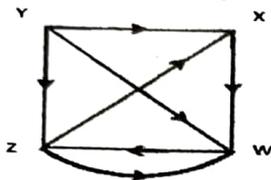
(5)

Q4 a) Solve the recurrence relation  $C_n = 6C_{n-1} - 11C_{n-2} + 6C_{n-3}$  for  $n \geq 3$ ,  
 $C_0 = 2, C_1 = 5, C_2 = 15$

(5)

b) Use Warshall's Algorithm to find matrix of a graph

(5)



Q5 a) Draw the Hasse Diagram of  $\{1, 2, 4, 5, 10, 20\}, /$  and Find is this poset a Lattice, if yes then find out the following subset set of given lattice is a sub lattice?

$A = \{2, 4, 10, 20\}, B = \{4, 5, 10, 20\}, C = \{1, 2, 5, 10\}$

(5)

b) Draw the graph of adjacency matrix also find degree of each vertex and find the incidence matrix of the given digraph.

(5)

	$e_1$	$e_2$	$e_3$	$e_4$	$e_5$	$e_6$
V1	1	0	0	0	1	0
V2	1	1	0	0	0	1
V3	-1	0	0	0	0	1
V4	0	0	1	1	0	1

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P-2/2